

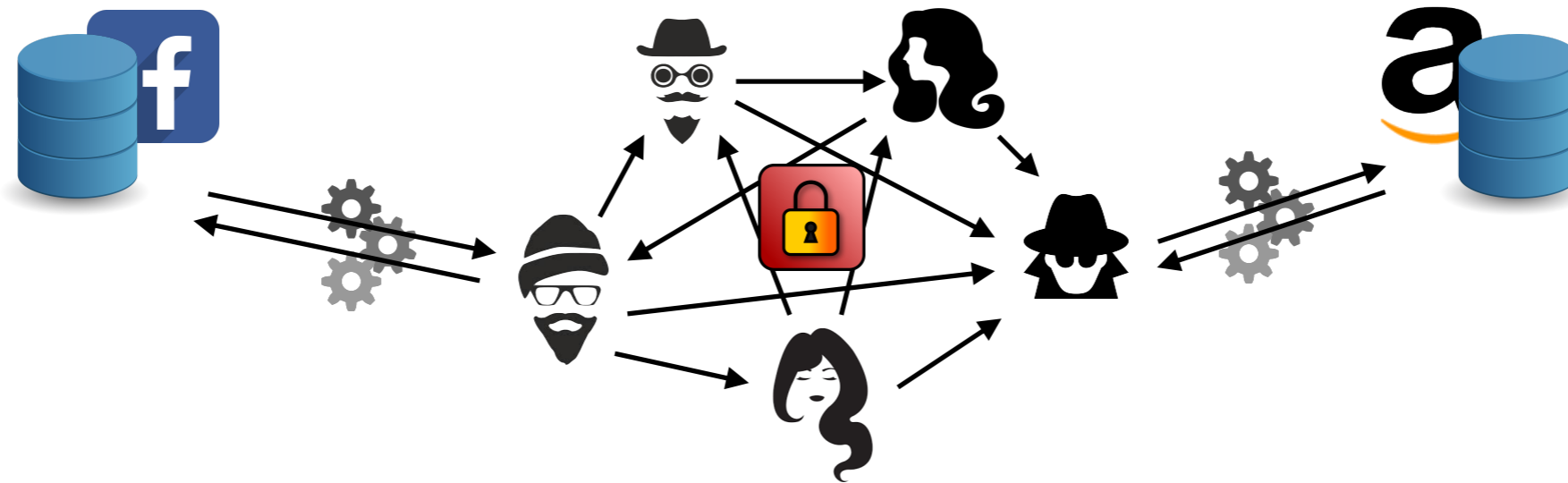
Efficient Two-Round OT Extension and Silent Non-Interactive Secure Computation



Elette Boyle, **Geoffroy Couteau**, Niv Gilboa, Yuval Ishai,
Lisa Kohl, Peter Rindal, Peter Scholl

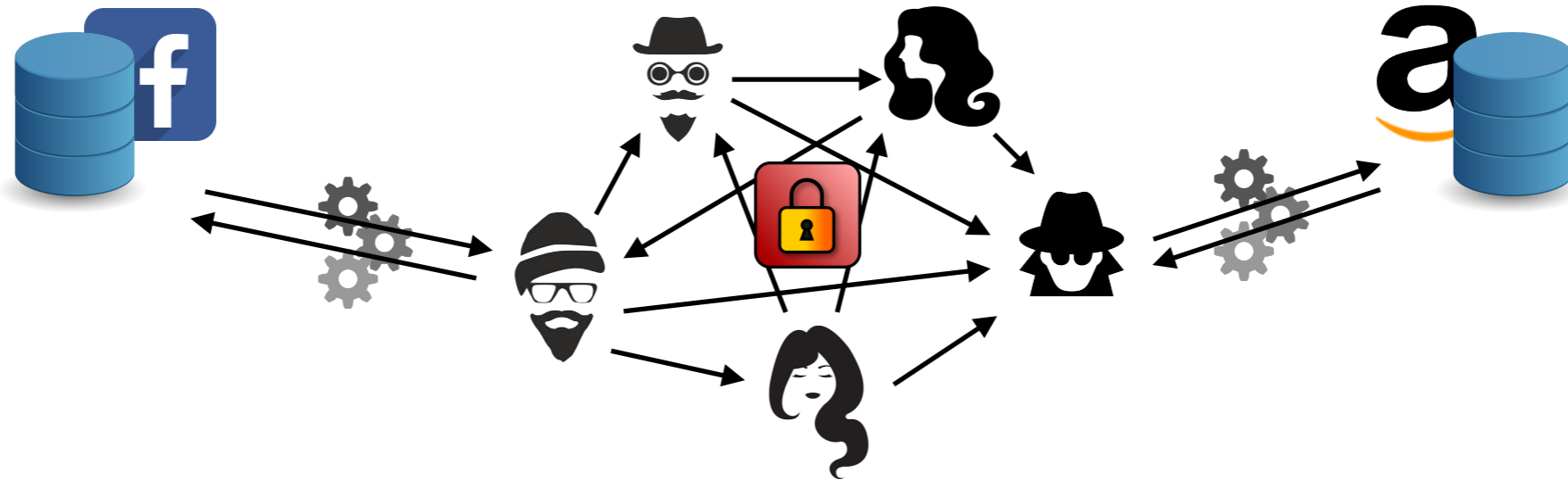
*Based on the results in [CCS:BCGIO17, CCS:BCGI18, CRYPTO:BCGIKS19,
CCS:BCGIKRS19, CRYPTO:BCGIKS20, FOCS:BCGIKS20]*

Secure Computation



Classical cryptography: protecting communications. However, data are not only *exchanged*: they are often *used in computations*.

Secure Computation

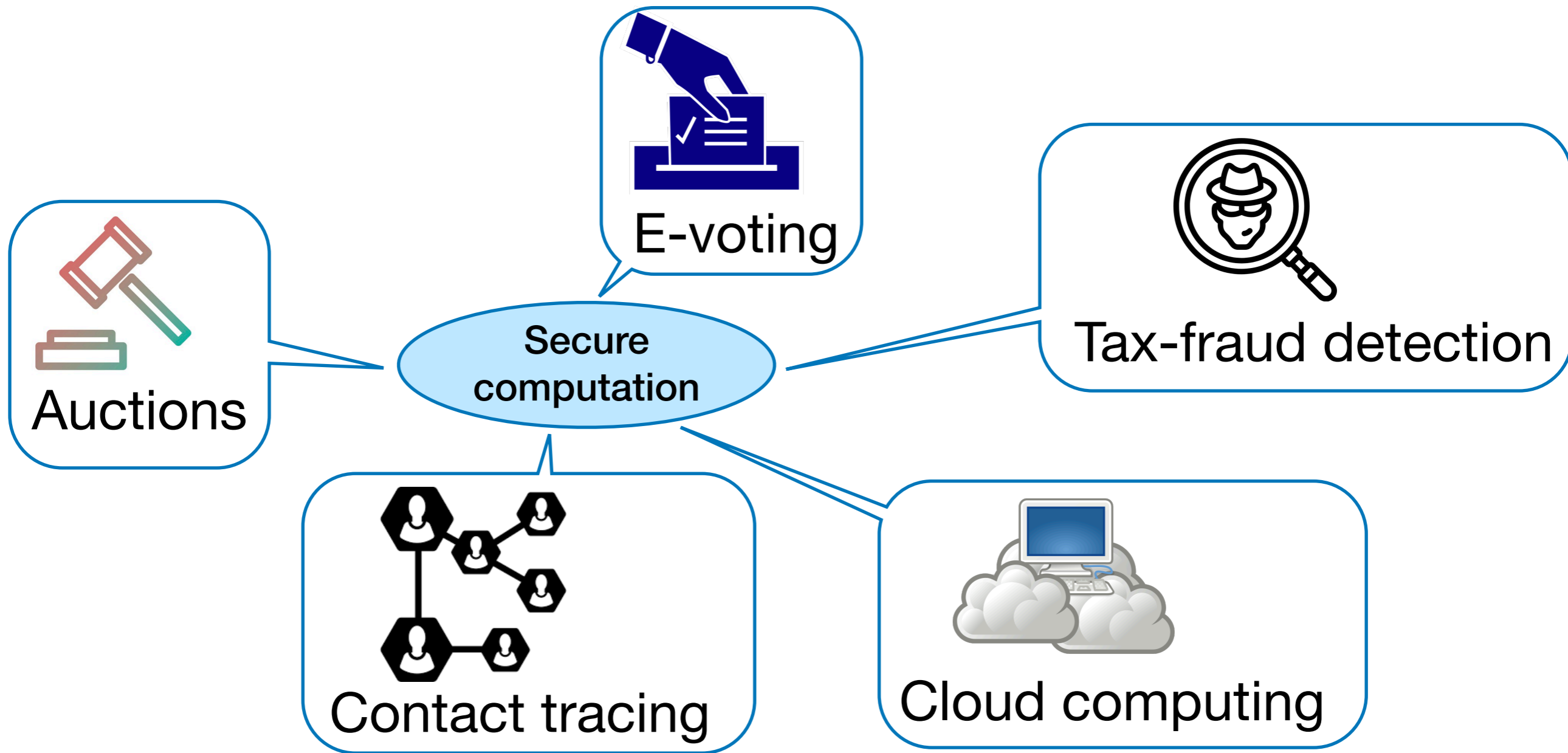


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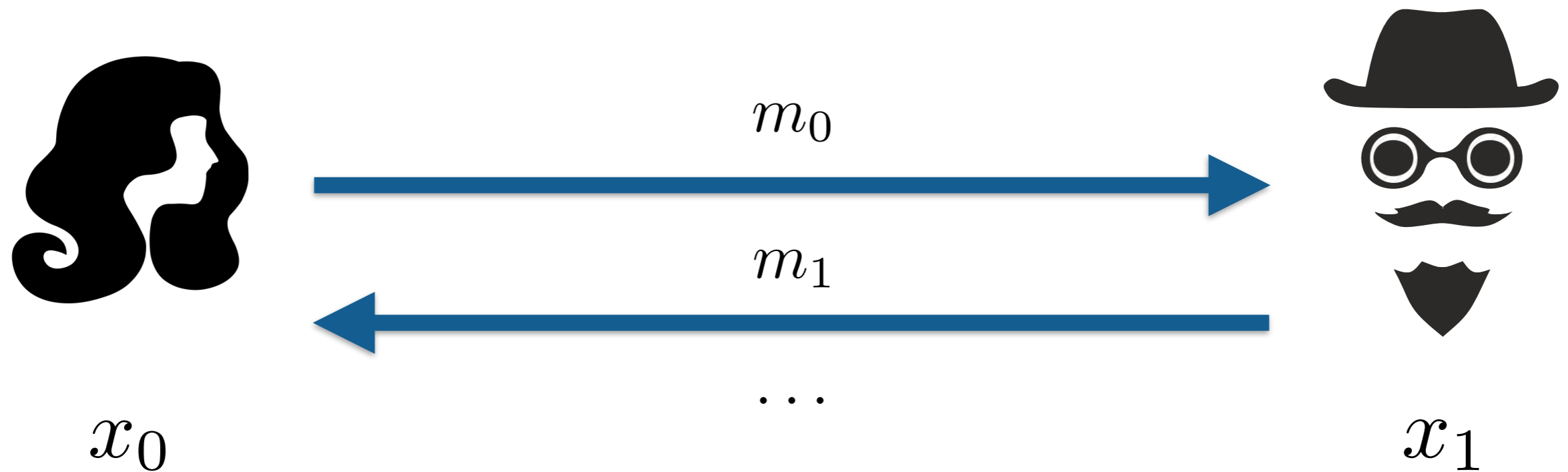
Is it possible to protect data privacy even when it's used in computations?

Secure Computation - Examples

Scenarios



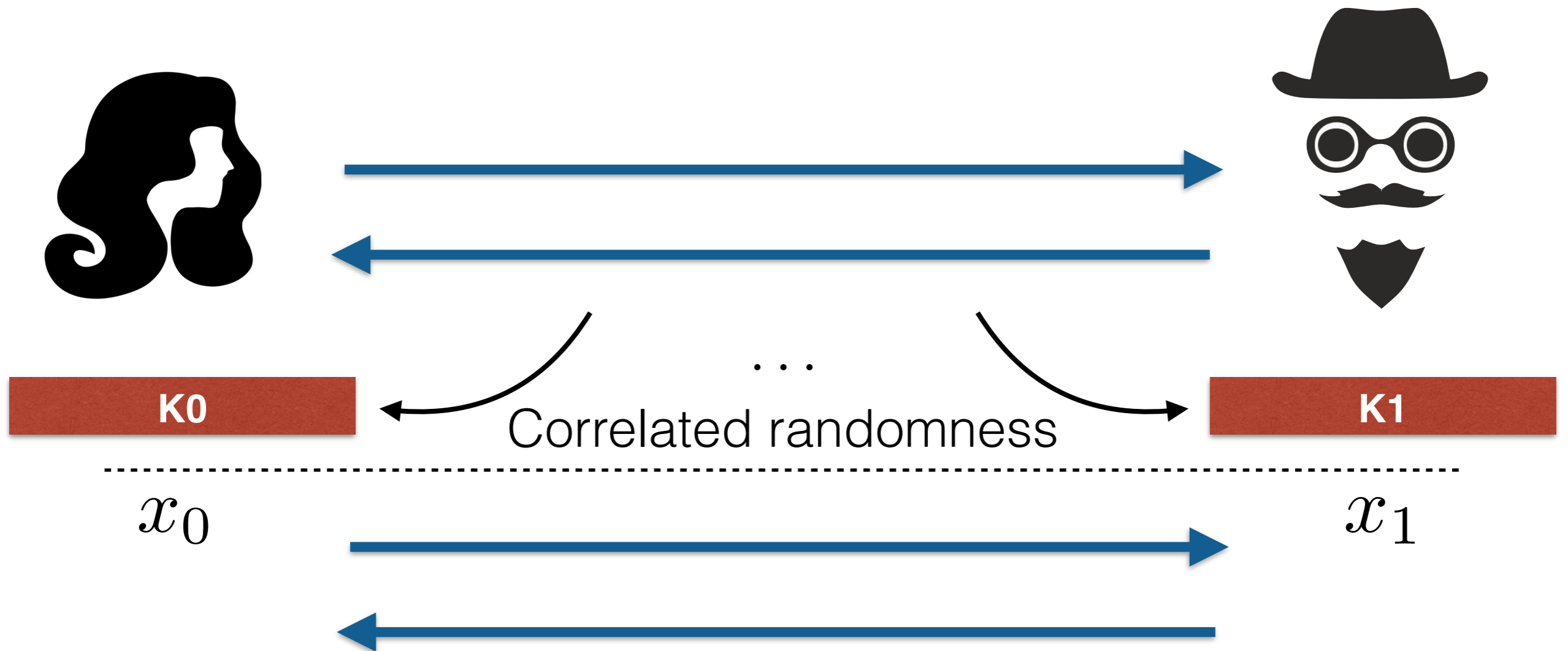
Secure 2-Party Computation



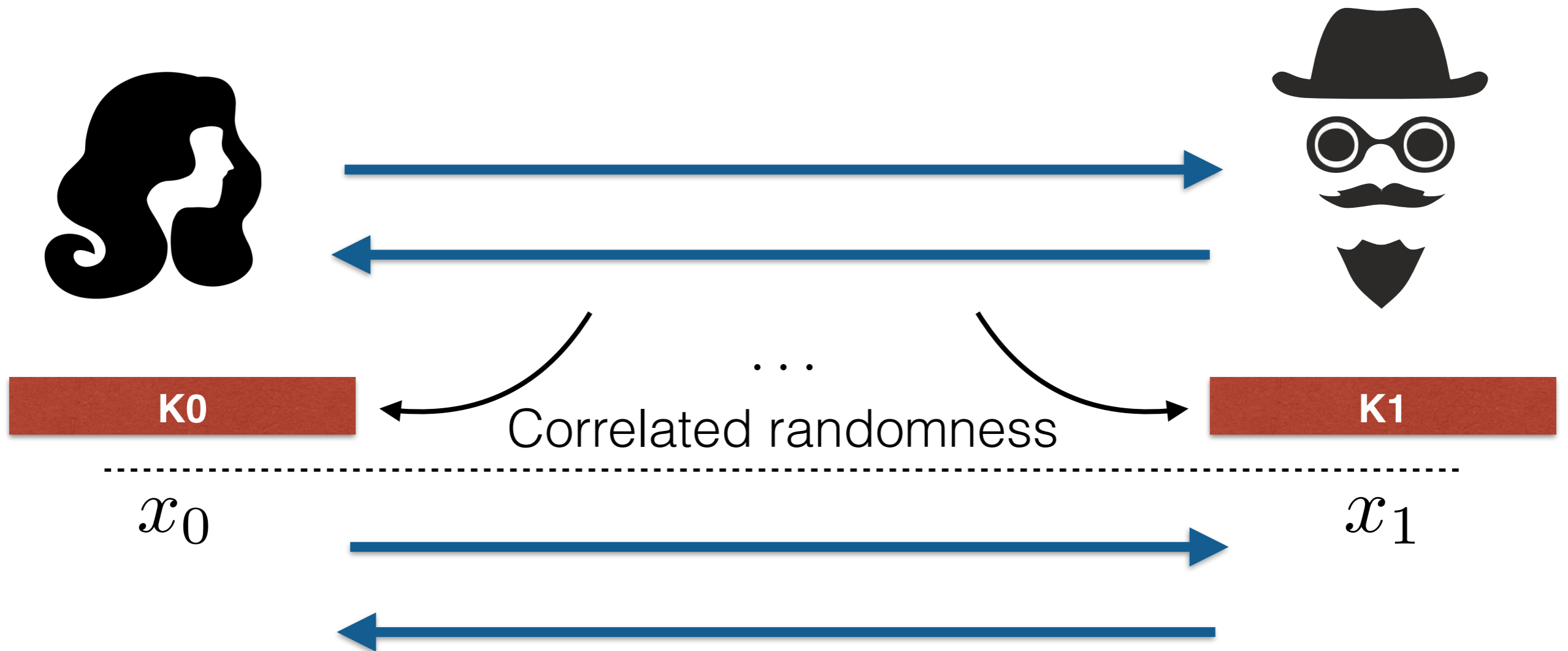
- both parties learn the output $f(x_0, x_1)$
- no party learns additional information

- ✓ (Yao, 1986) Can evaluate any poly time function
- ✗ Computationally expensive

Secure 2-Party Computation in the Preprocessing Model



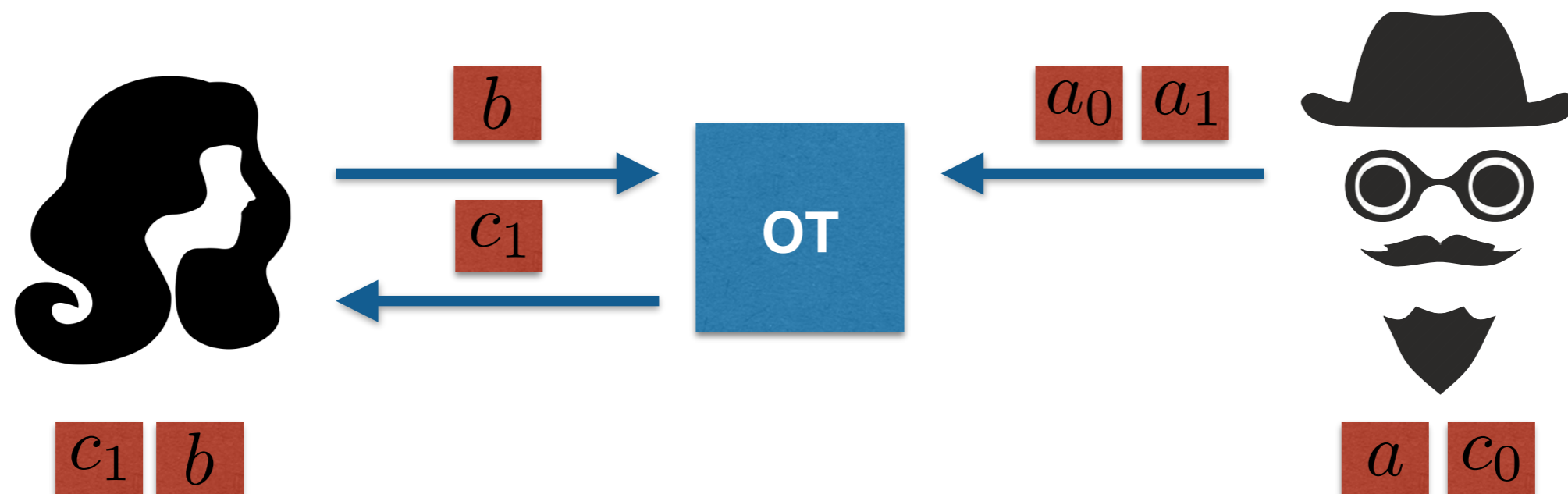
Secure 2-Party Computation in the Preprocessing Model



- ✓ Fast, information-theoretic online phase
- ✓ Security against dishonest majority
- ✗ Expensive preprocessing (storage and communication)

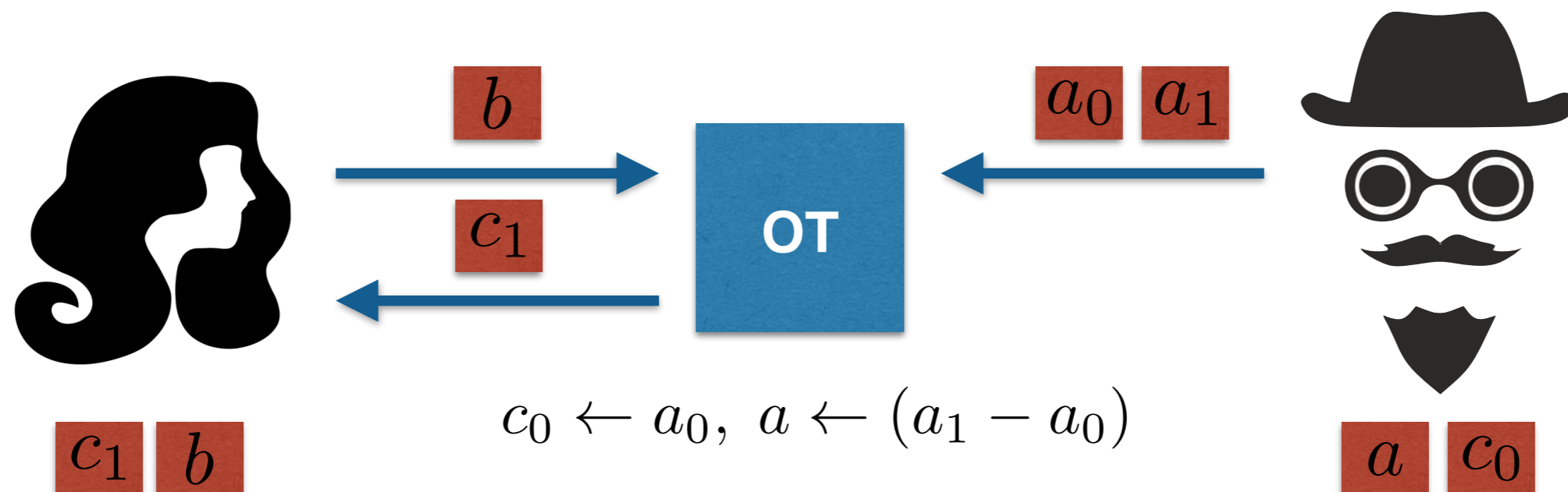
Example of a Useful Correlation: Oblivious Transfer

Security. Alice learns only c_1 , Bob learns nothing



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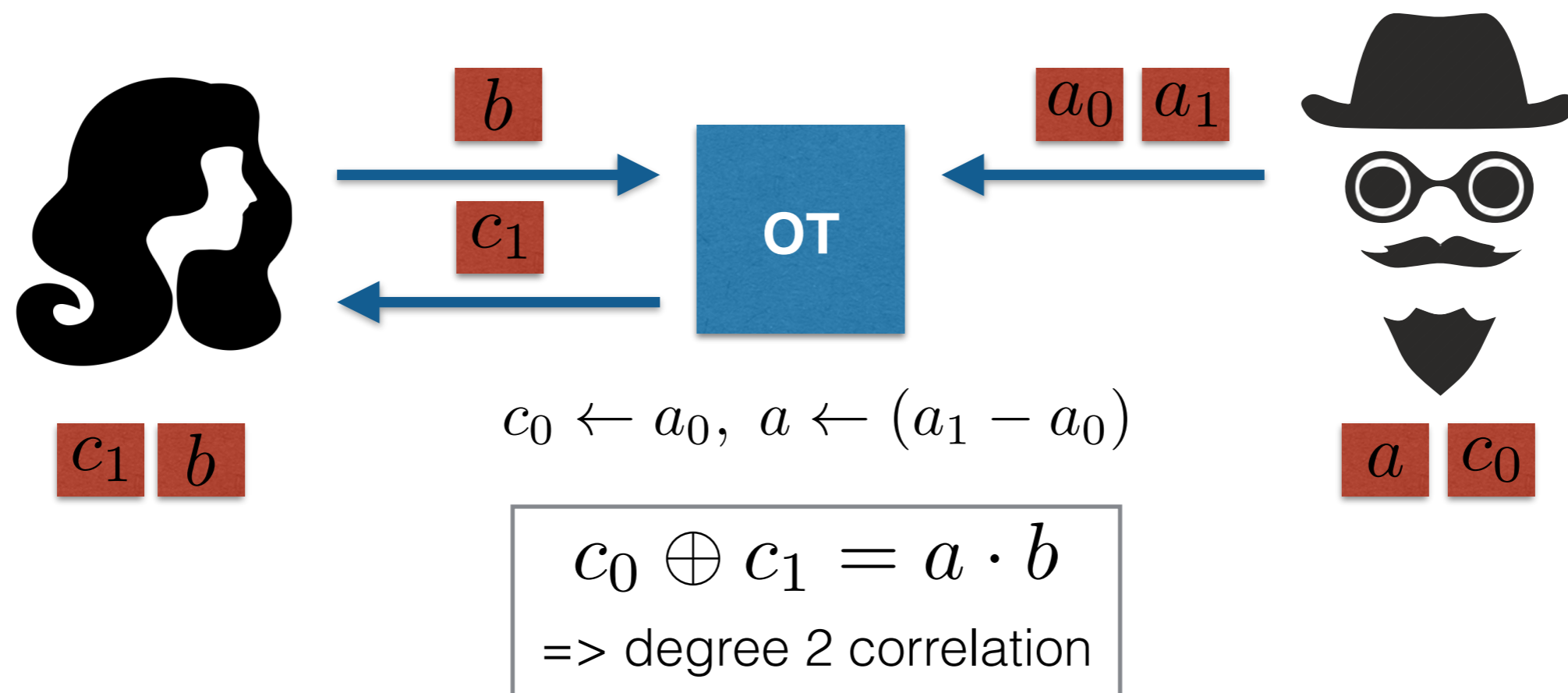
$$c_0 \leftarrow a_0, a \leftarrow (a_1 - a_0)$$

$$c_0 \oplus c_1 = a \cdot b$$

=> degree 2 correlation

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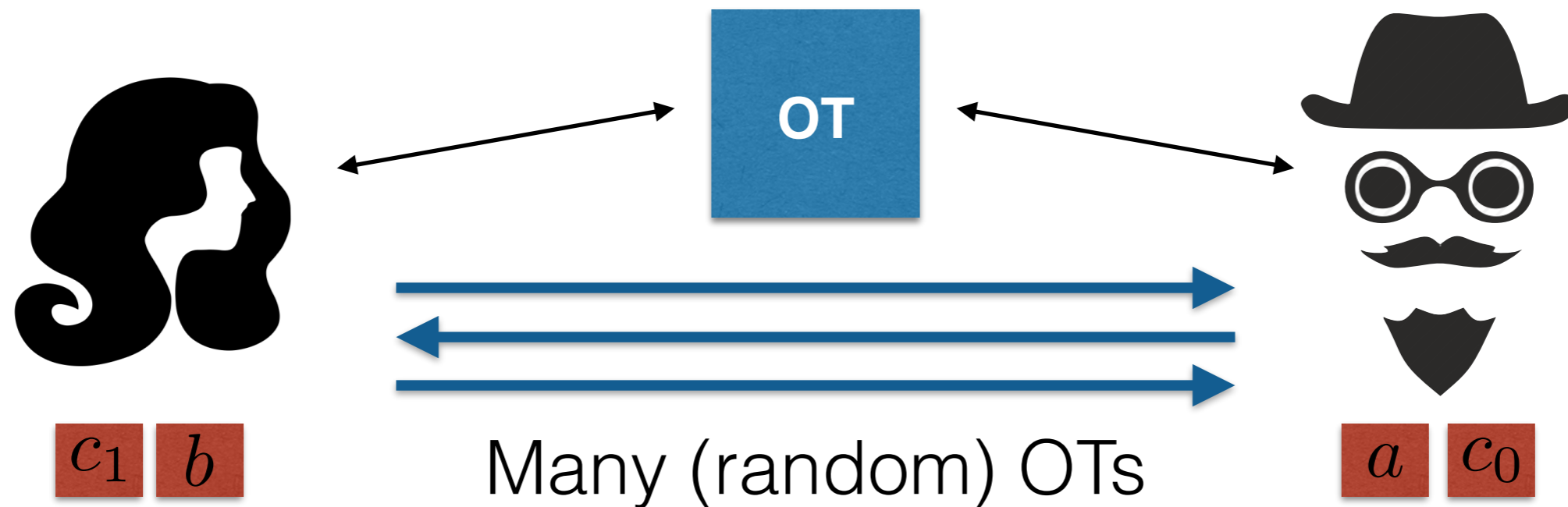
GMW Protocol. 2 OT per AND gate

Problem. OT is expensive (public-key primitive)

OT Extension

[Bea96, IKNP03]

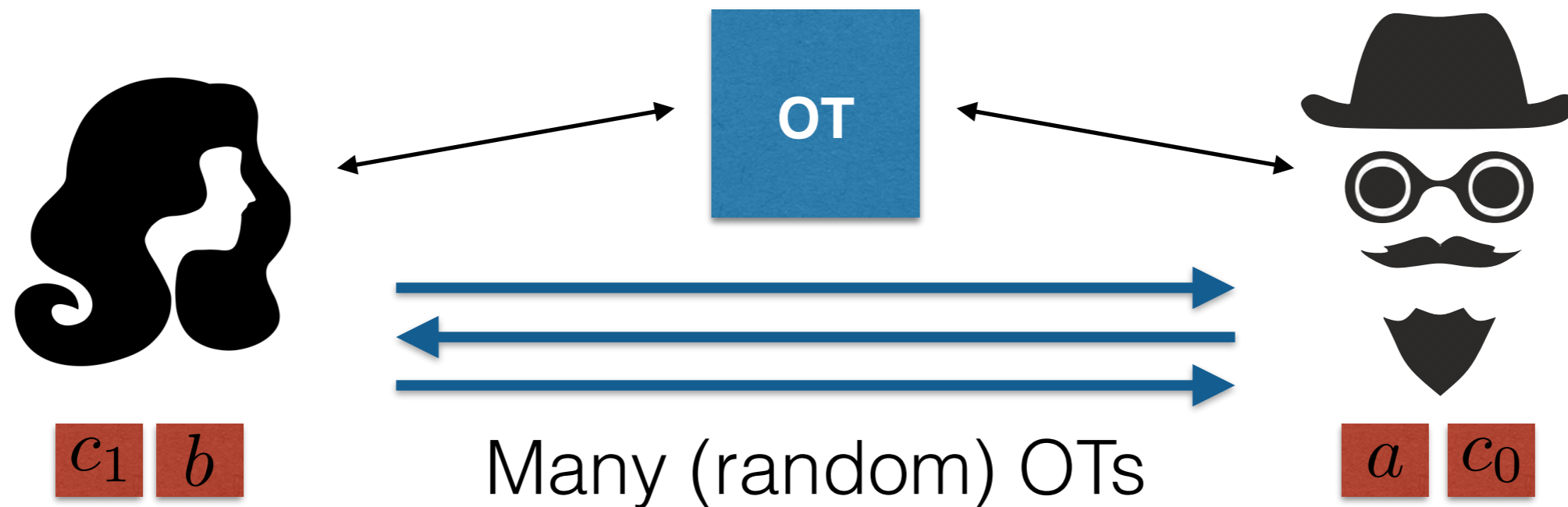
Hybrid Approach. Few base OTs + symmetric crypto



OT Extension

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Hybrid Approach. Few base OTs + symmetric crypto

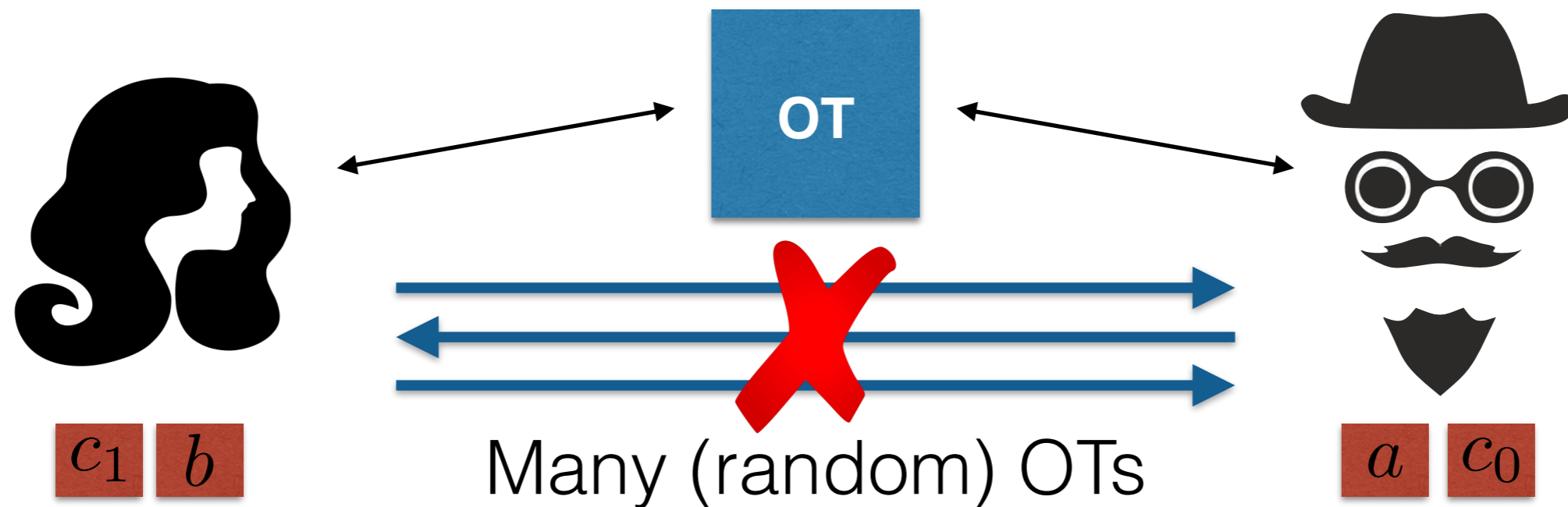


Problem. Communication & storage linear in #OTs

OT Extension

[Bea96, IKNP03]

Hybrid Approach. Few base OTs + symmetric crypto

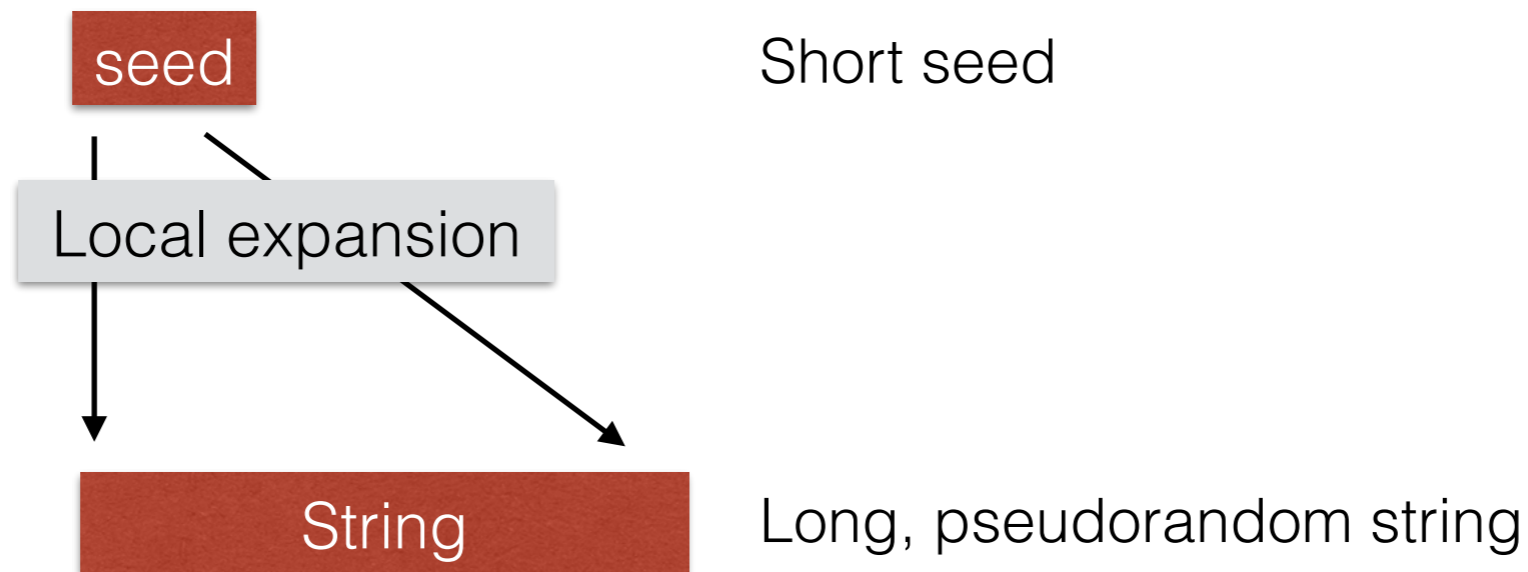


Problem. Communication & storage linear in #OTs

Silent OT Extension. Communication & storage *sublinear*

Pseudorandom Generator

$$\text{PRG} : \{0, 1\}^n \mapsto \{0, 1\}^m \text{ with } m \gg n$$

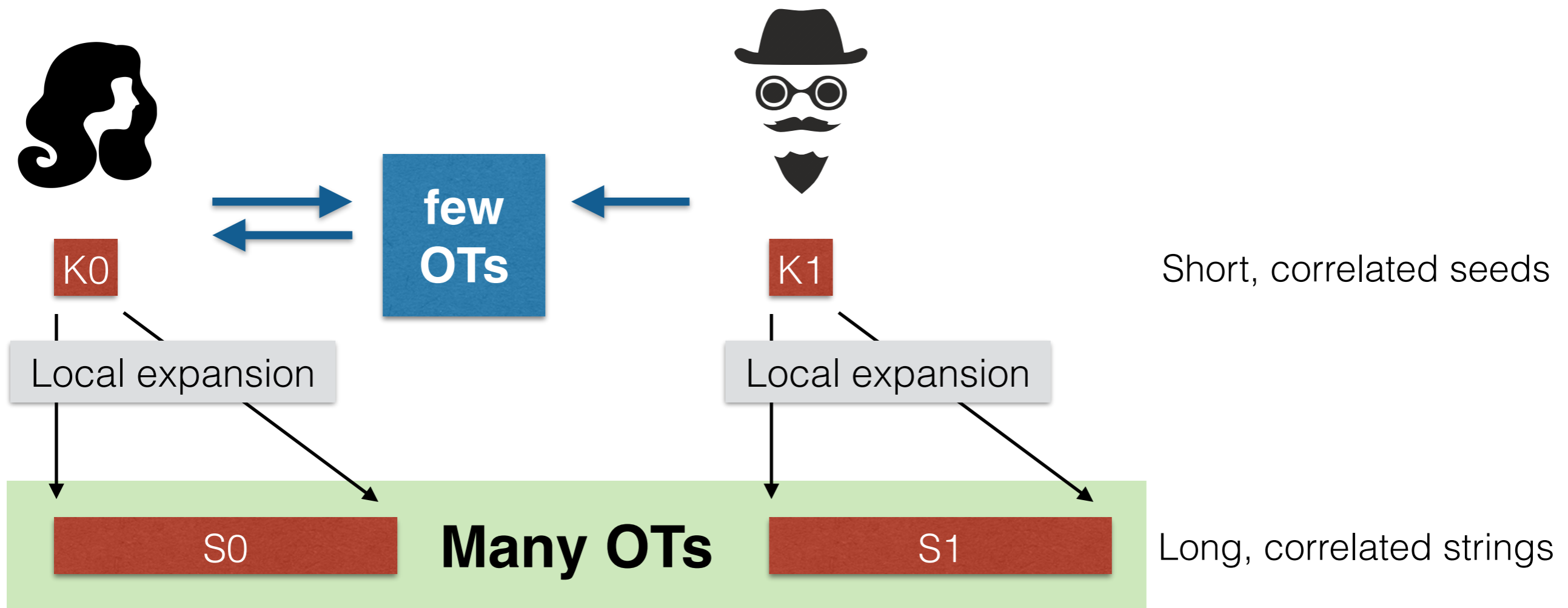


Formally, \forall PPT \mathcal{A} ,

$$|\Pr[y \leftarrow_{\$} \{0, 1\}^m : \mathcal{A}(y) = 1]| - \Pr[x \leftarrow_{\$} \{0, 1\}^n, y \leftarrow \text{PRG}(x) : \mathcal{A}(y) = 1]| \approx 0$$

Pseudorandom Correlation Generator (PCG)

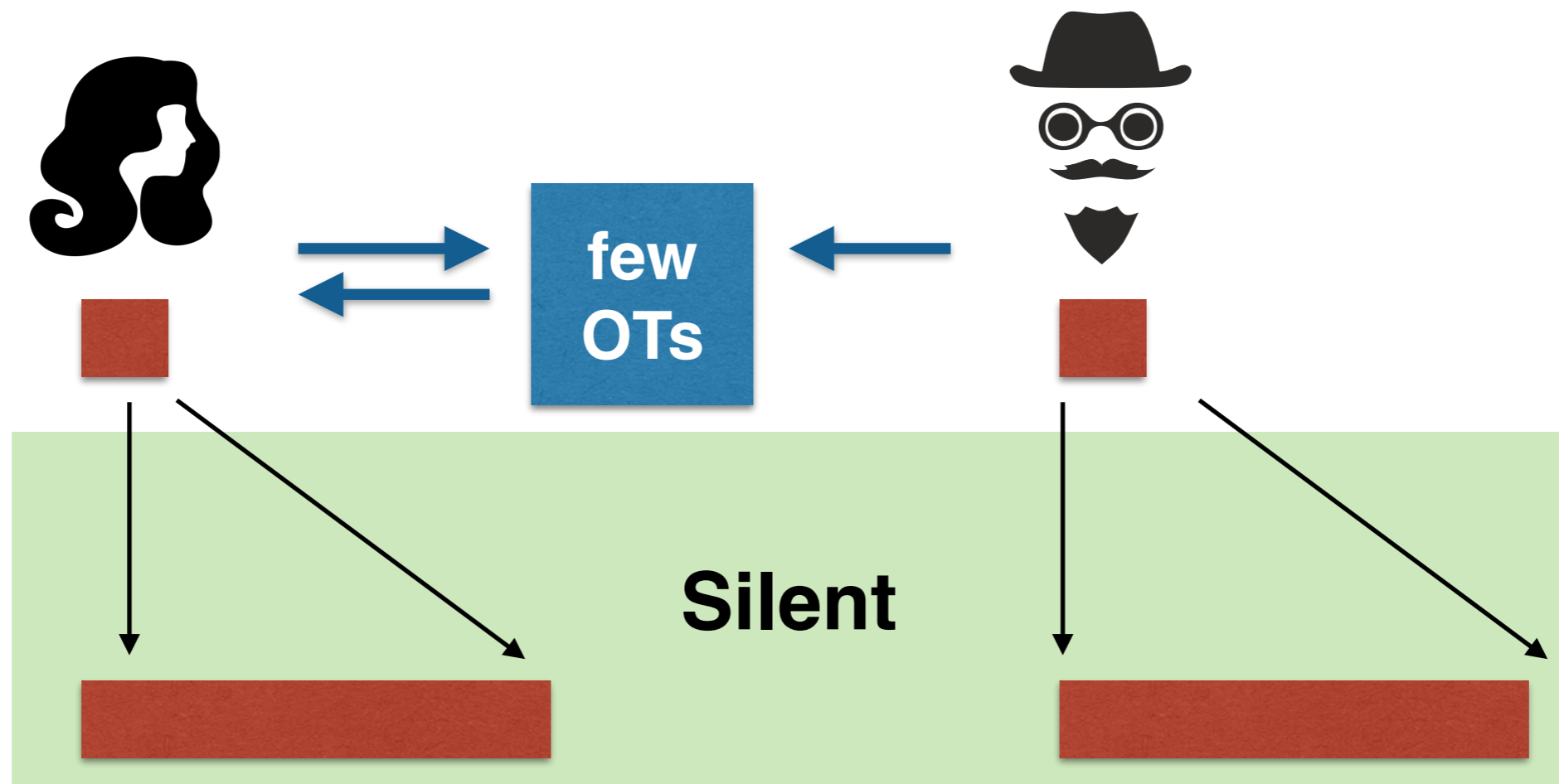
[BCGI18,BCGIKS19]



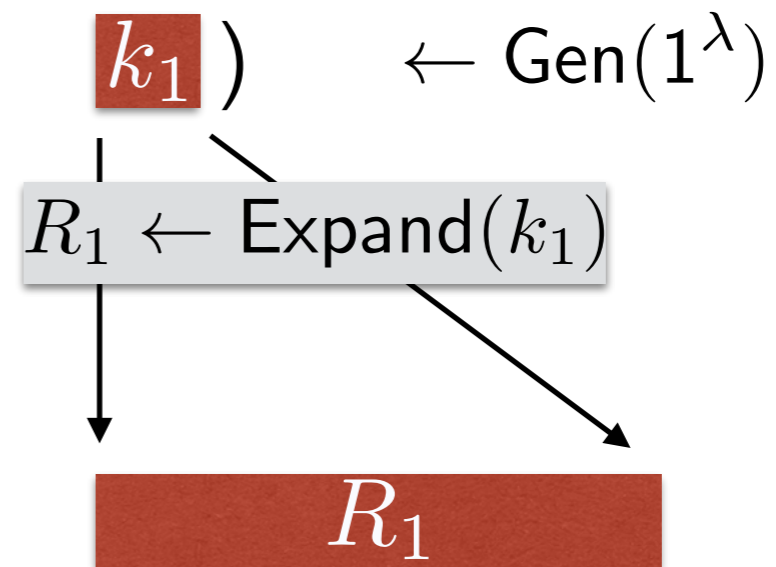
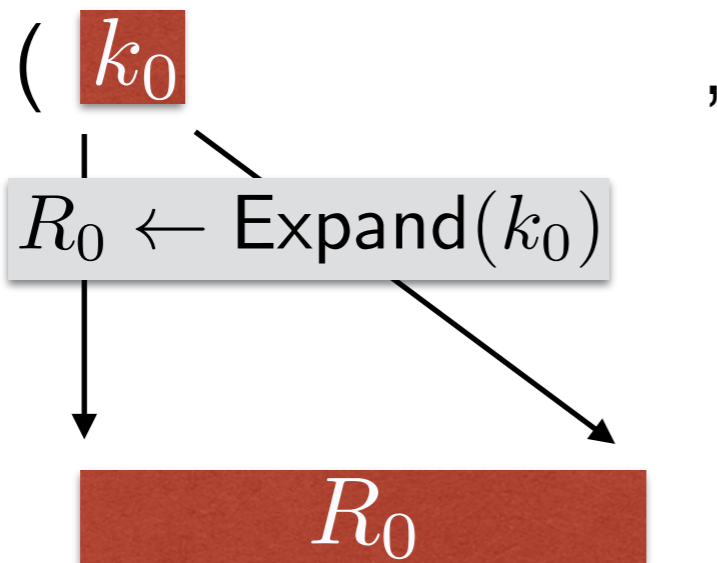
Pseudorandom Correlation Generator (PCG)

[BCGI18,BCGIKS19]

PCGs have the **silent** feature.



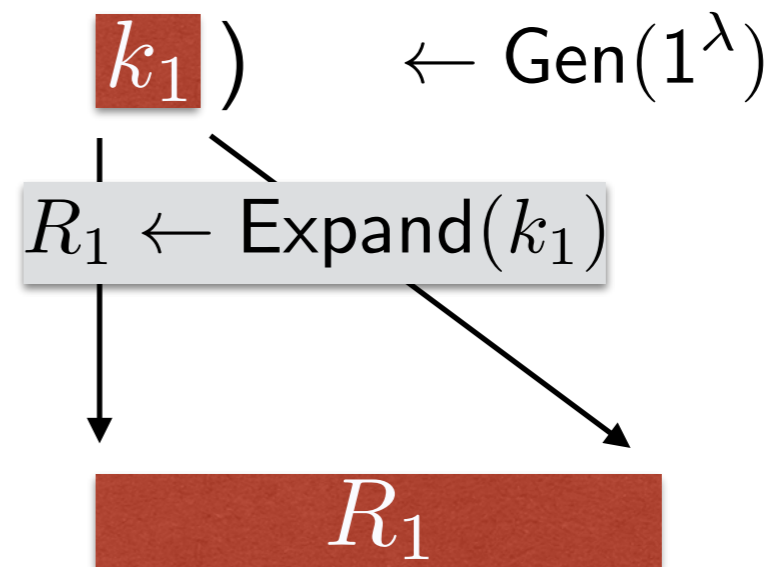
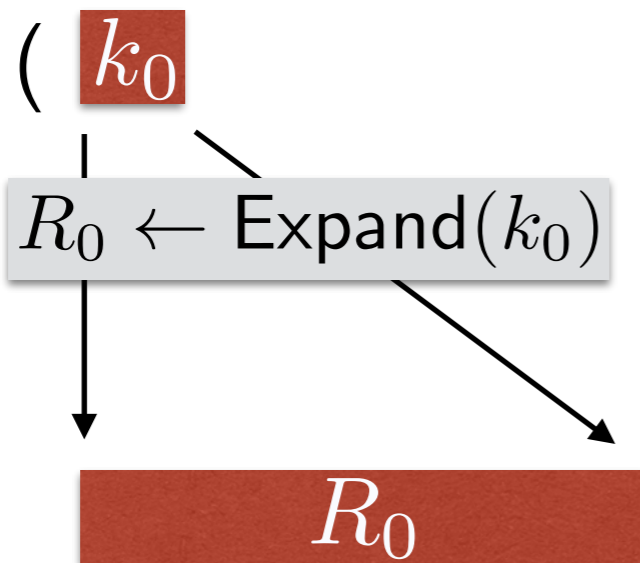
PCG Definition



Correctness. $\text{rel}(R_0, R_1) = 1$

Security. $(k_0, R_1) \approx (k_0, [R_1 \text{ random s.t. } \text{rel}(R_0, R_1) = 1])$
+ Expand is a PRG

PCG Definition



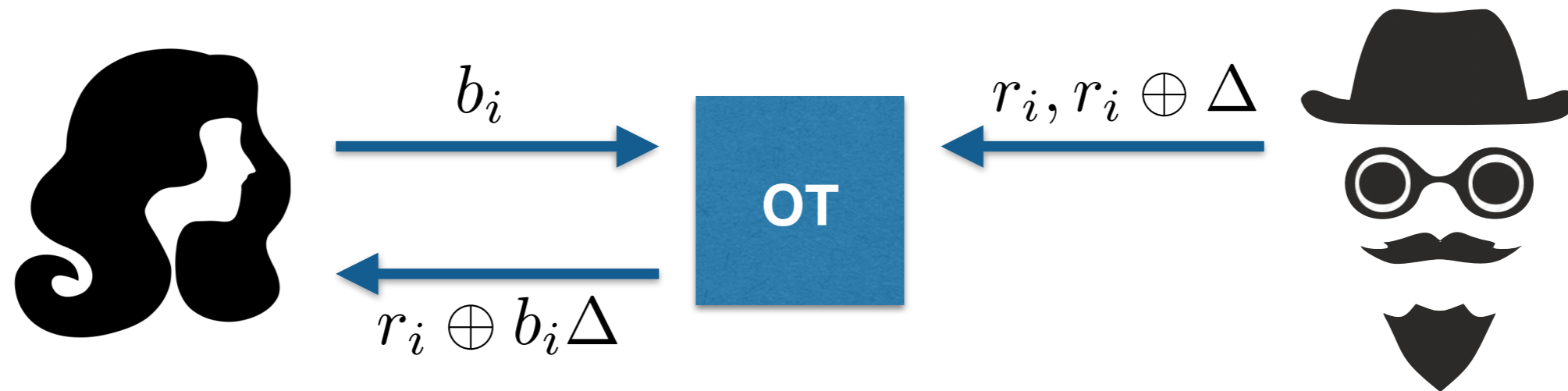
Plug-and-play: can we use PCG to generate preprocessing material?

We show several impossibility results (e.g. randomized functionalities) and some positive results (**corruptible** functionalities)

Towards Silent OT Extension

[CCS:BCGIKS18, CRYPTO:BCGIKS19, CCS:BCGIKRS19]

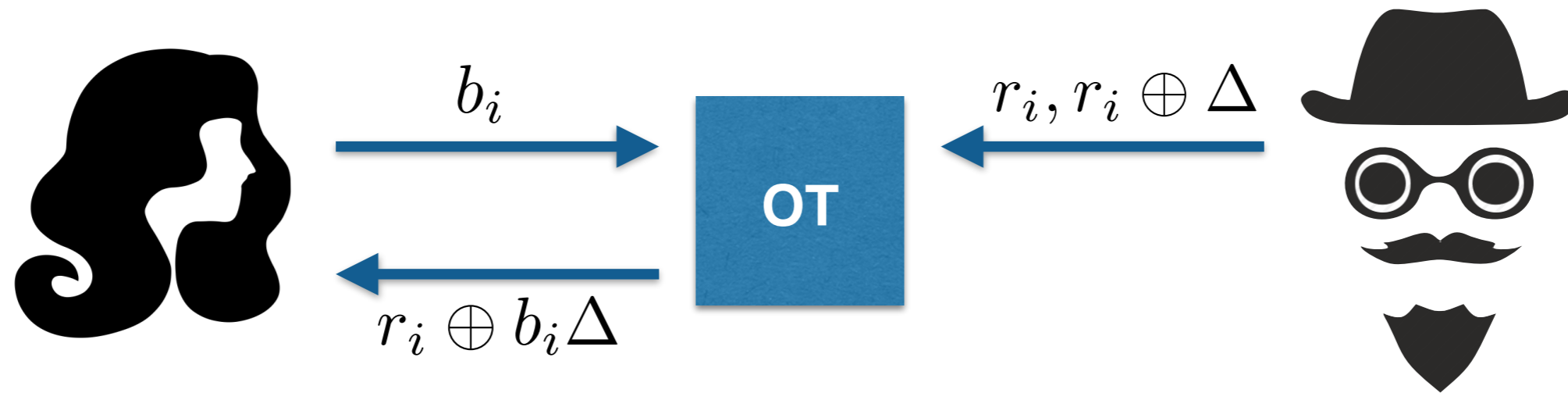
Correlated OT:



Towards Silent OT Extension

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Correlated OT:



Correlated OT + correlation-robust hash functions \Rightarrow OT [IKNP03]

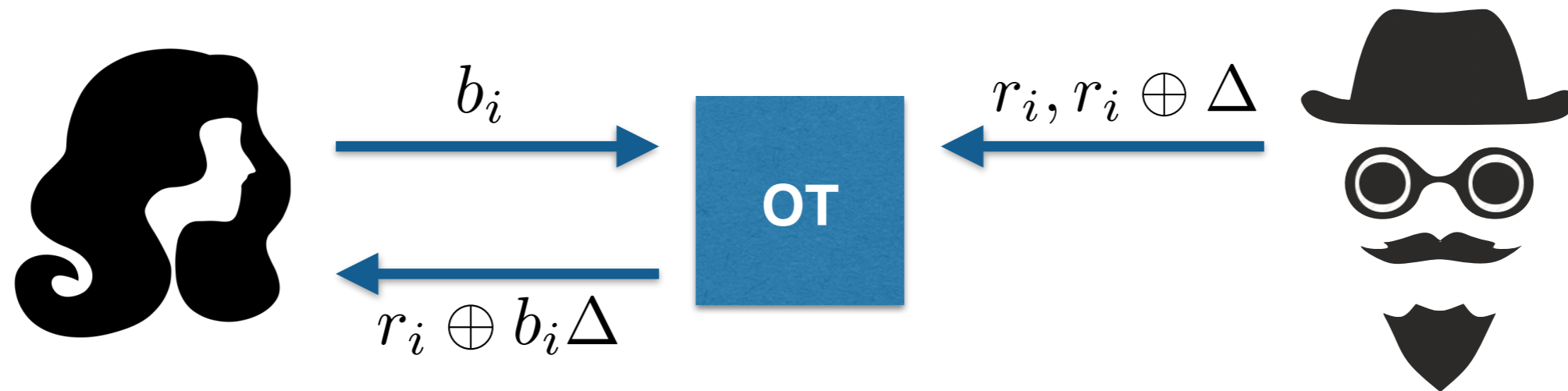
$$H(r_i \oplus b_i \Delta)$$

$$H(r_i), H(r_i \oplus \Delta)$$

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$$H(r_i), H(r_i \oplus \Delta)$$

Rephrasing correlated OT:

$$\begin{aligned} (\vec{r} \oplus \vec{b} \cdot \Delta) \oplus \vec{r} &= \vec{b} \cdot \Delta \\ \implies \vec{q} \oplus \vec{r} &= \vec{b} \cdot \Delta \end{aligned}$$

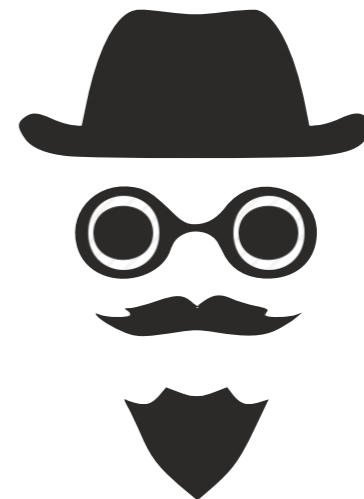
PCG for Correlated OT - Strategy

Correlated OT:



\vec{q}, \vec{b}

$$\vec{q} \oplus \vec{r} = \vec{b} \cdot \Delta$$



\vec{r}, Δ

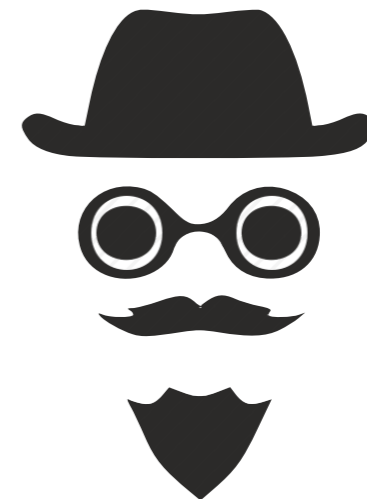
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Correlated OT:



\vec{q}, \vec{b}

$$\underbrace{\vec{q} \oplus \vec{r} = \vec{b} \cdot \Delta}_{\text{additive shares of } \vec{b} \cdot \Delta}$$



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Goal: compressing \vec{q}, \vec{b} and \vec{r}, Δ

PCG for Correlated OT - Strategy

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Goal: compressing \vec{q}, \vec{b} and \vec{r}, Δ

Roadmap:

PPRFs

PCG for a unit vector $\vec{b} \cdot \Delta$

Summation

PCG for a sparse $\vec{b} \cdot \Delta$

Syndrome decoding

PCG for a pseudorandom $\vec{b} \cdot \Delta$

First Tool: Puncturable PRFs

PRF:

A function sampled from $\mathcal{F} = \{F_k\}_k$
is indistinguishable from a truly random
function (via black-box access)

First Tool: Puncturable PRFs

Puncturable PRF (PPRF):

$$F_k: \{1, \dots, N\} \rightarrow \mathbb{F}_{2^\lambda}$$

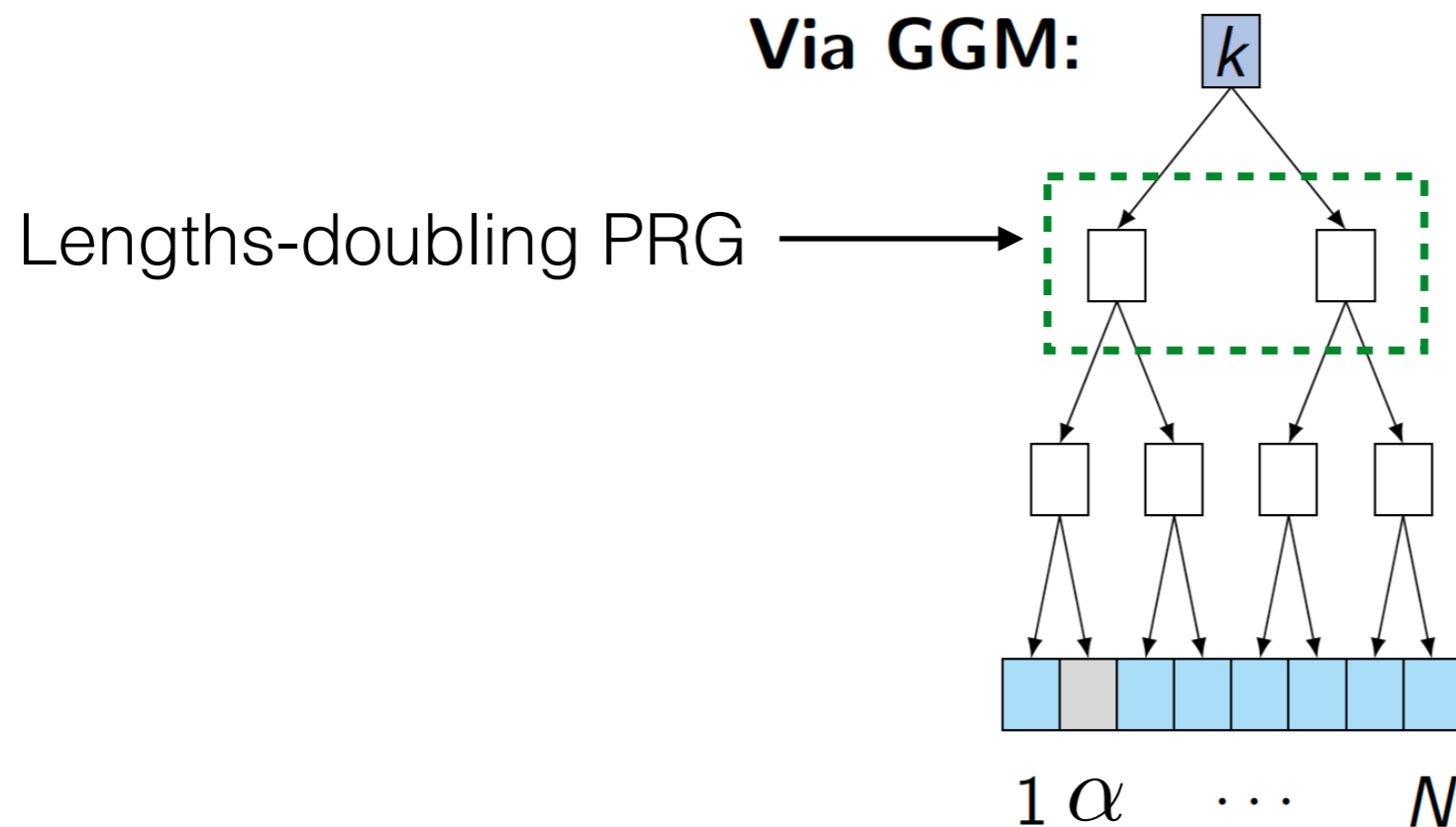
- ▶ $k \rightsquigarrow F_k(x)$ for all x
 - ▶ $k^* \rightsquigarrow F_k(x)$ for all $x \neq \alpha$
-

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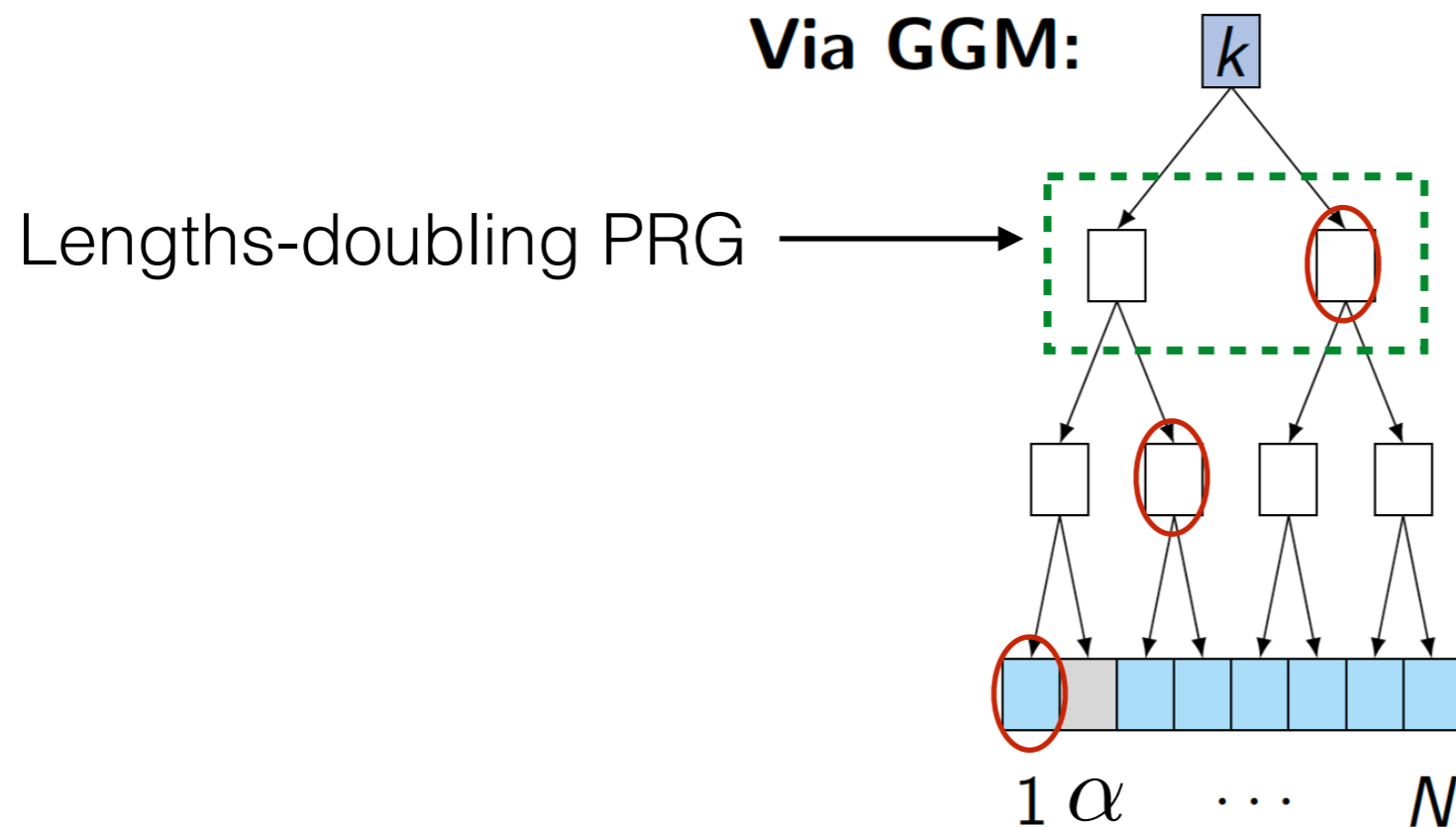


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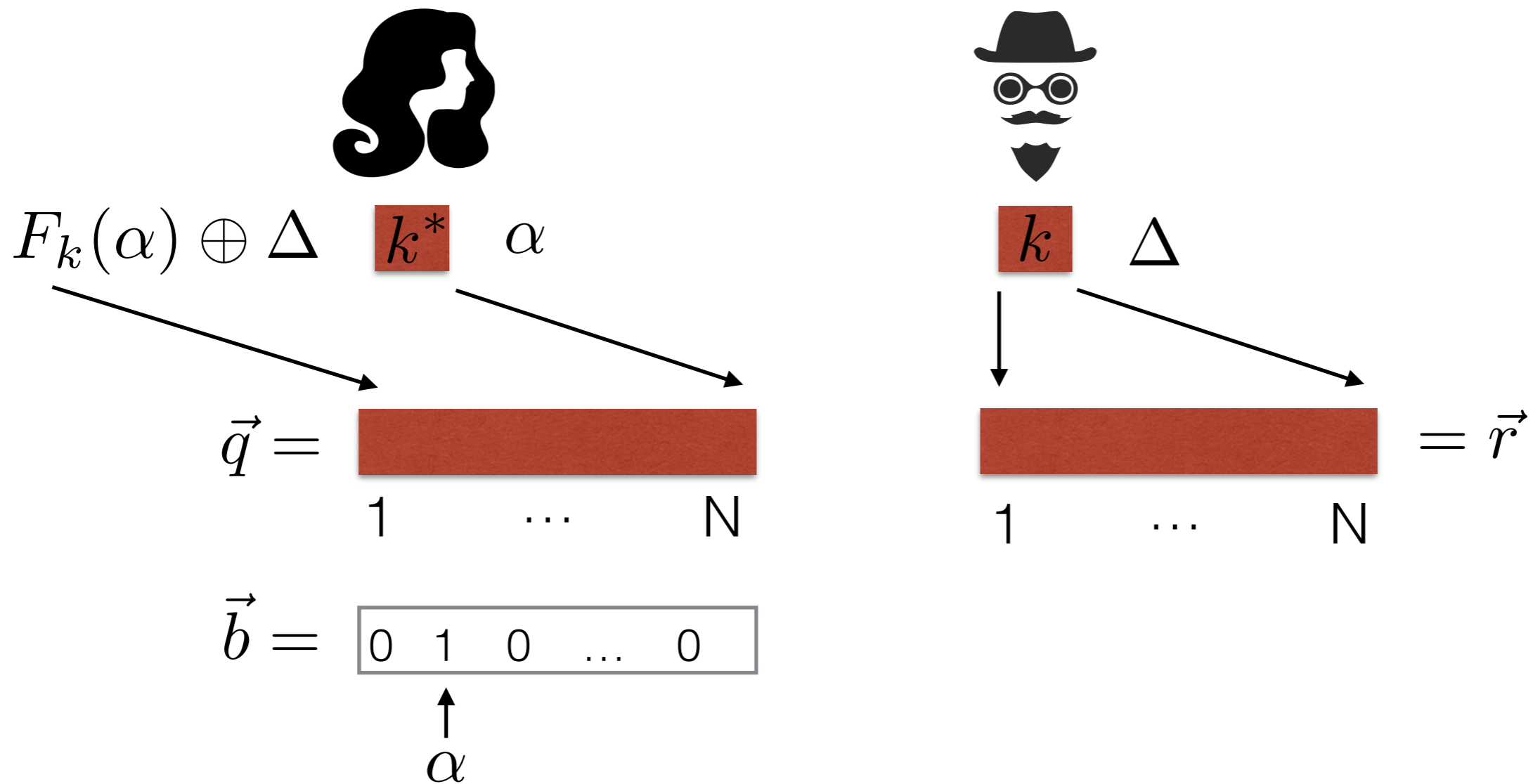
Puncturable PRF (PPRF):

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PCG for Unit Vectors via PPRFs

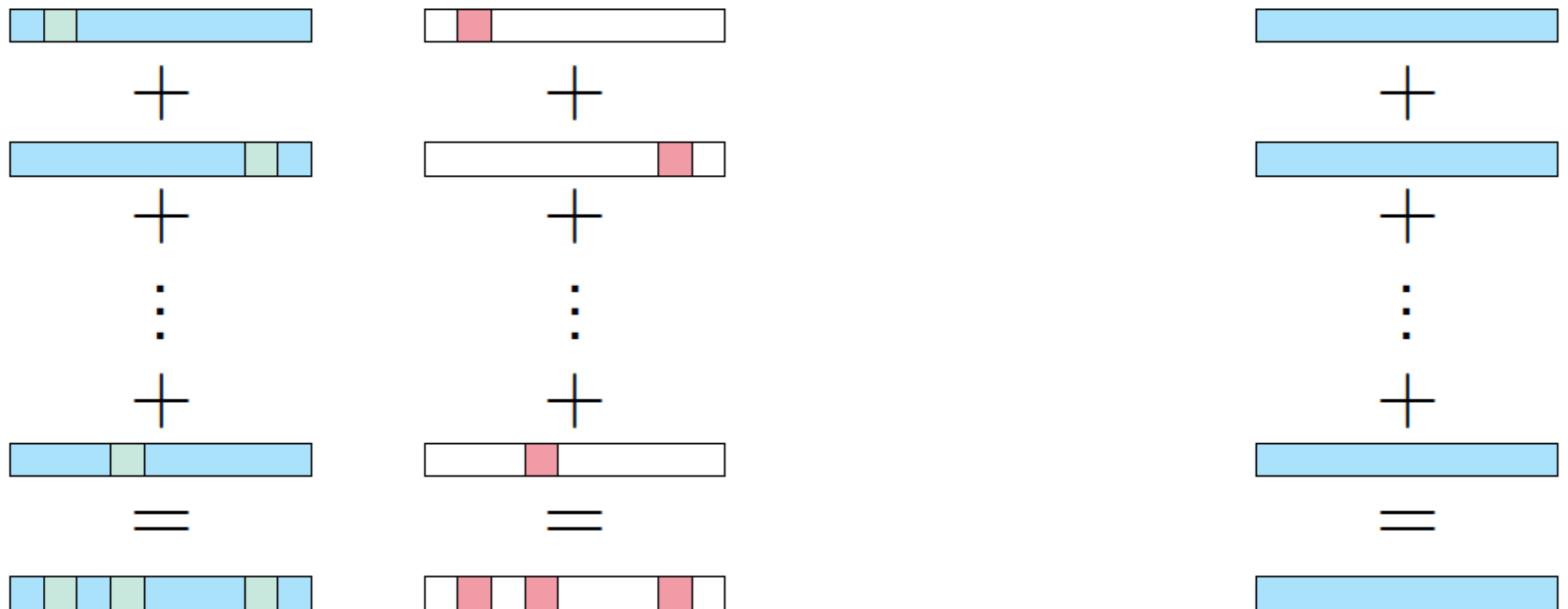


$$\vec{q} \oplus \vec{r} = \vec{b} \cdot \Delta$$

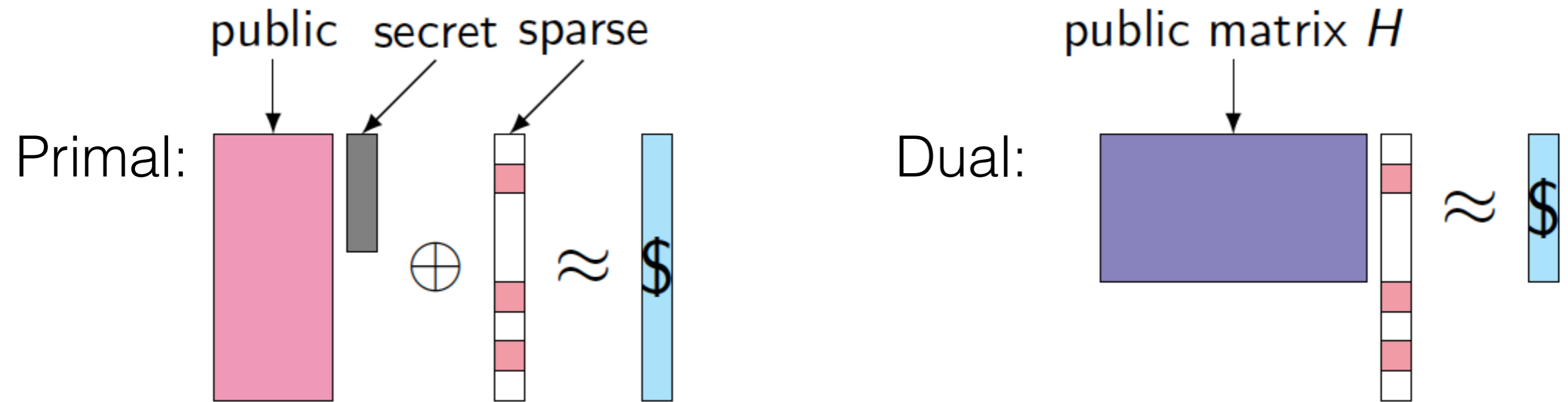
From Unit Vectors to Sparse Vectors via Addition

PCG for unit vectors \Rightarrow PCG for weight-t vectors

by t-fold repetition of the unit vector version:



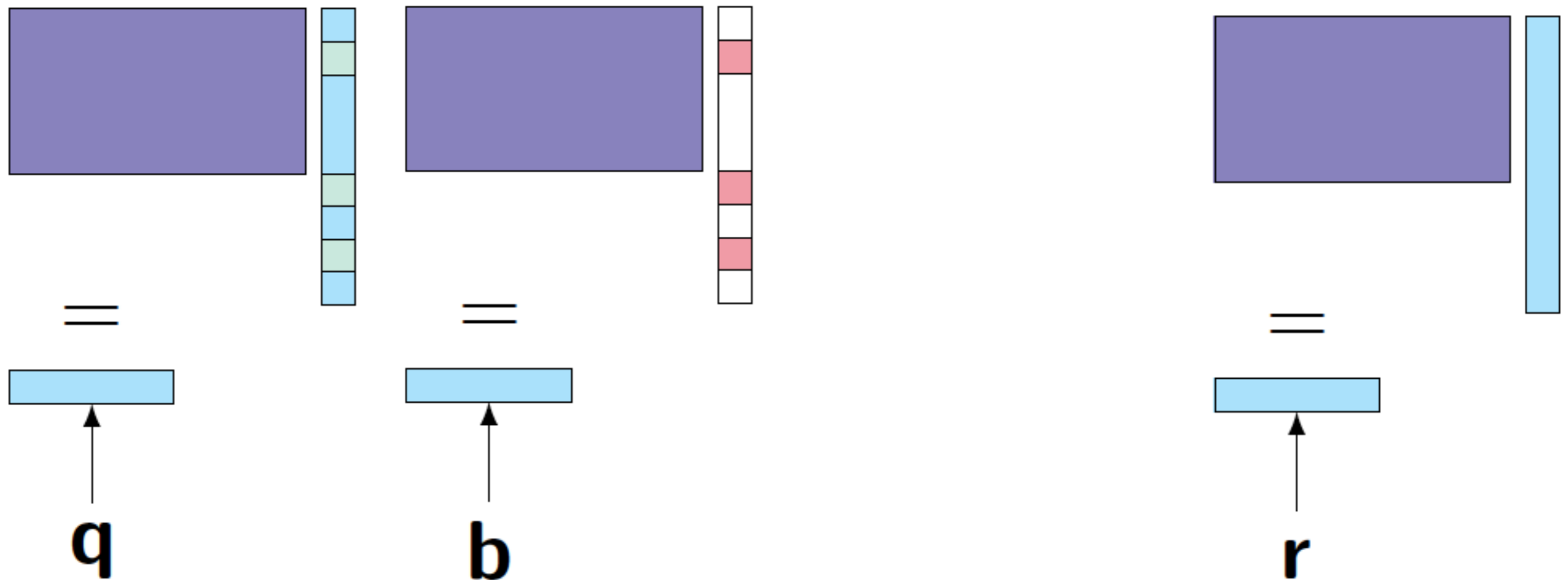
Syndrome Decoding (SD)



Notes:

- Security is similar to PQ cryptosystems e.g. BIKE, HQC [AAB+19, ABB+19]
- Not known to imply PKE for certain noise rates

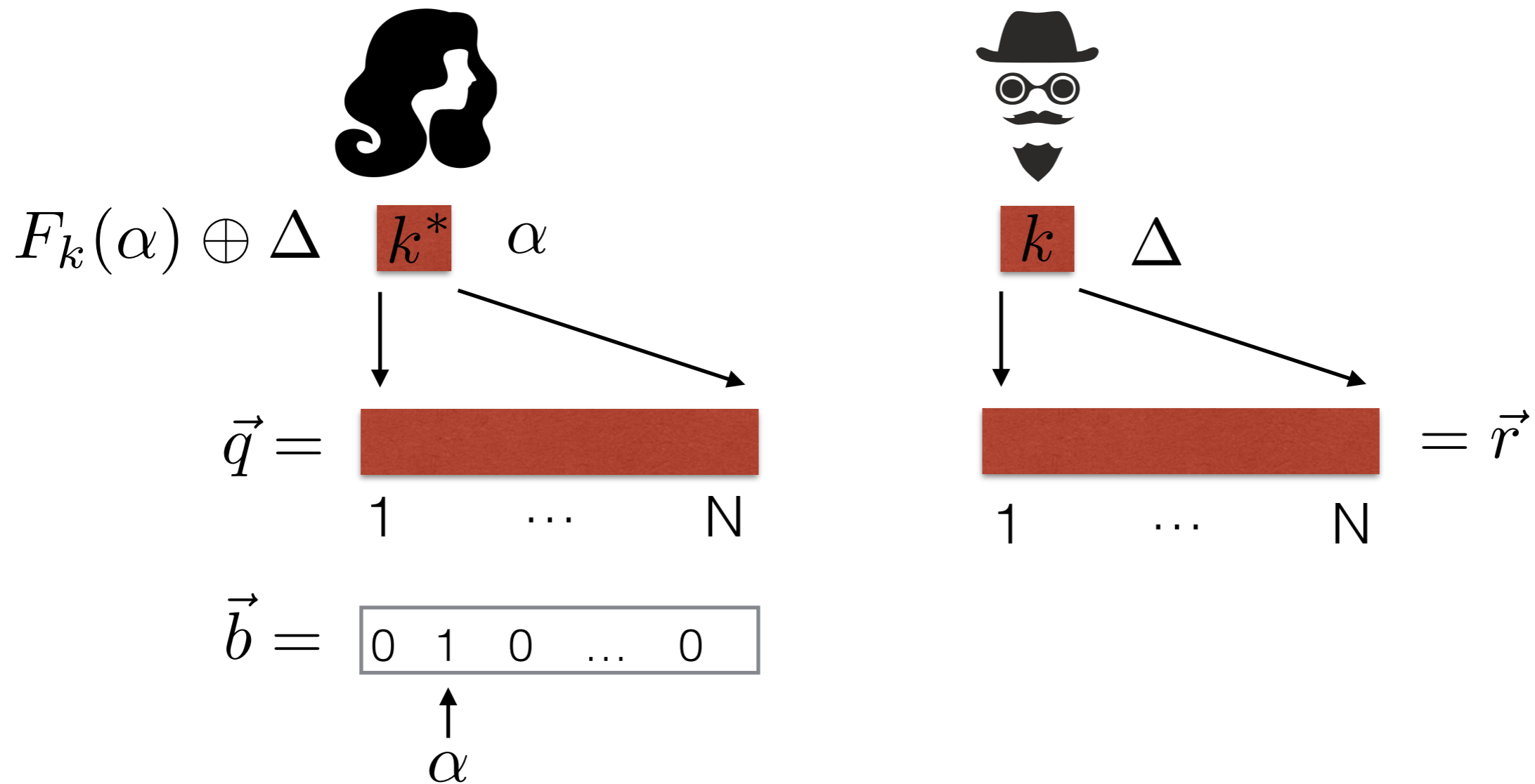
From Sparse to Pseudorandom via SD



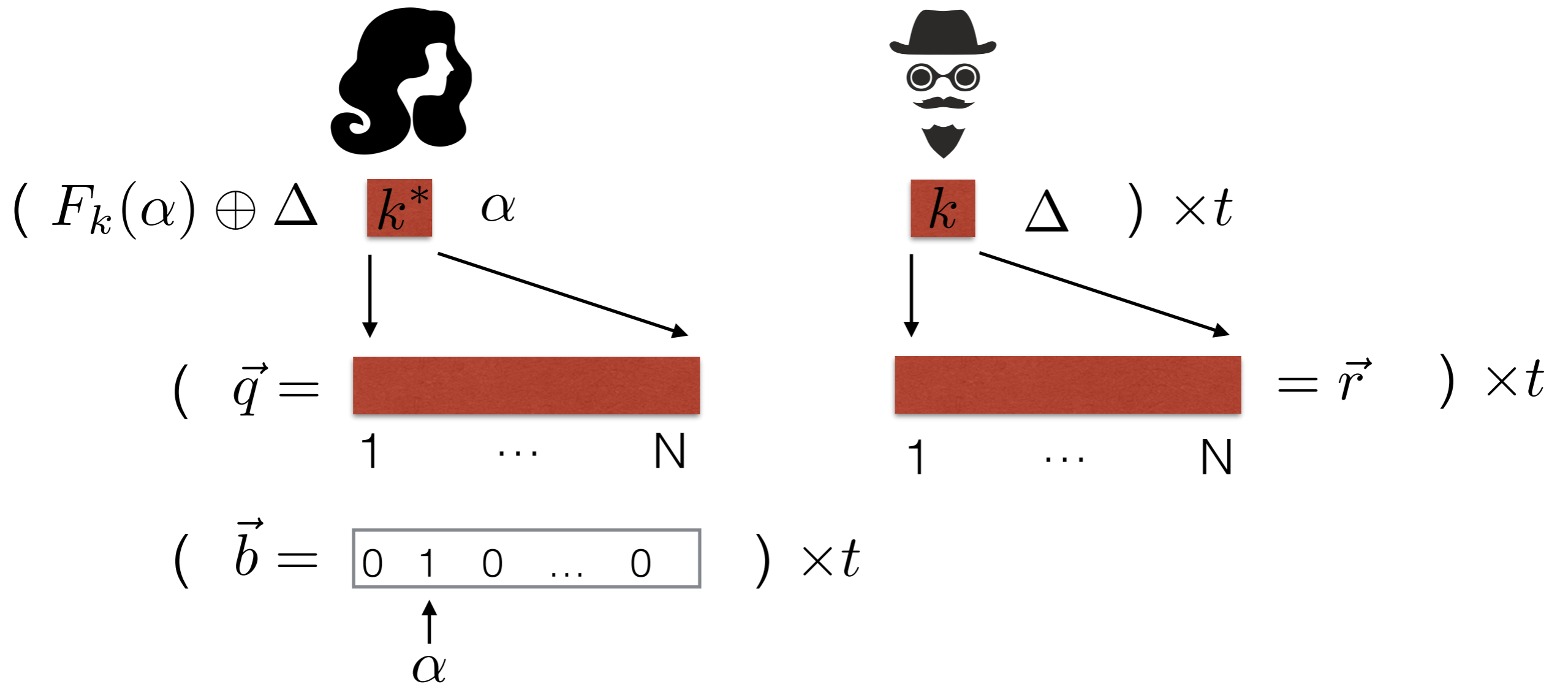
By correctness of DPF + linearity of addition + linearity of SD:

$$\vec{q} \oplus \vec{r} = \vec{b} \cdot \Delta$$

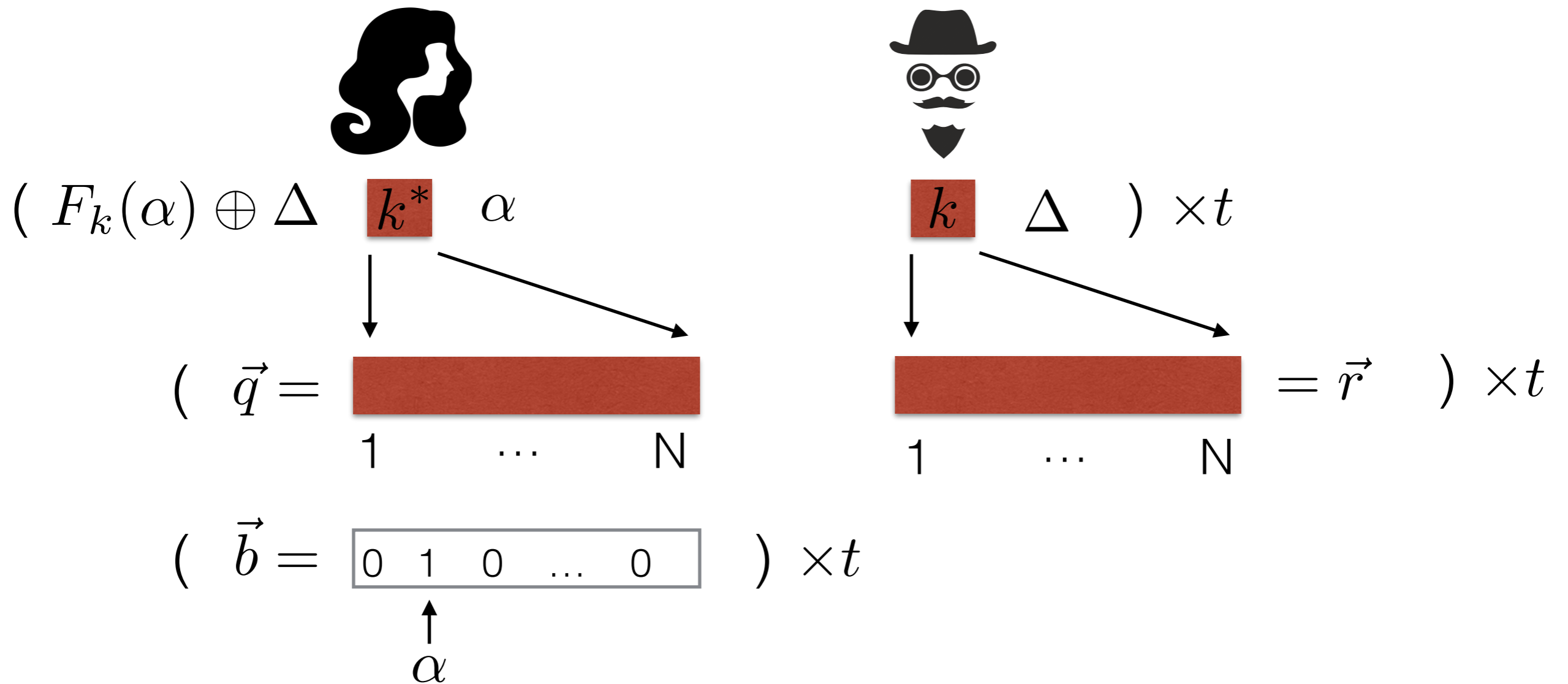
Wrapping Up - PCG for Correlated OT



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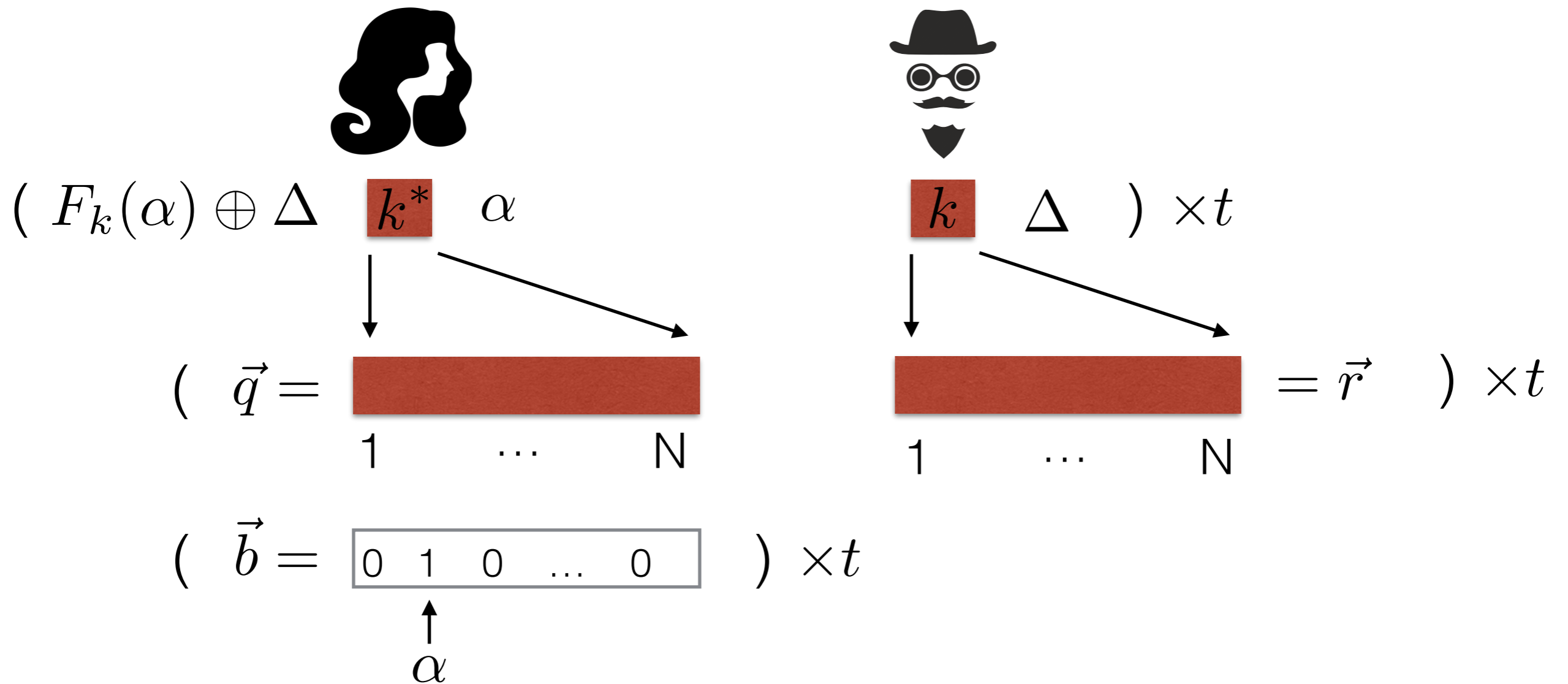


Wrapping Up - PCGG for Correlated OT



Then sum and multiply by public matrices to get dense vectors
Security: provably reduces to syndrome decoding

Wrapping Up - PCG for Correlated OT

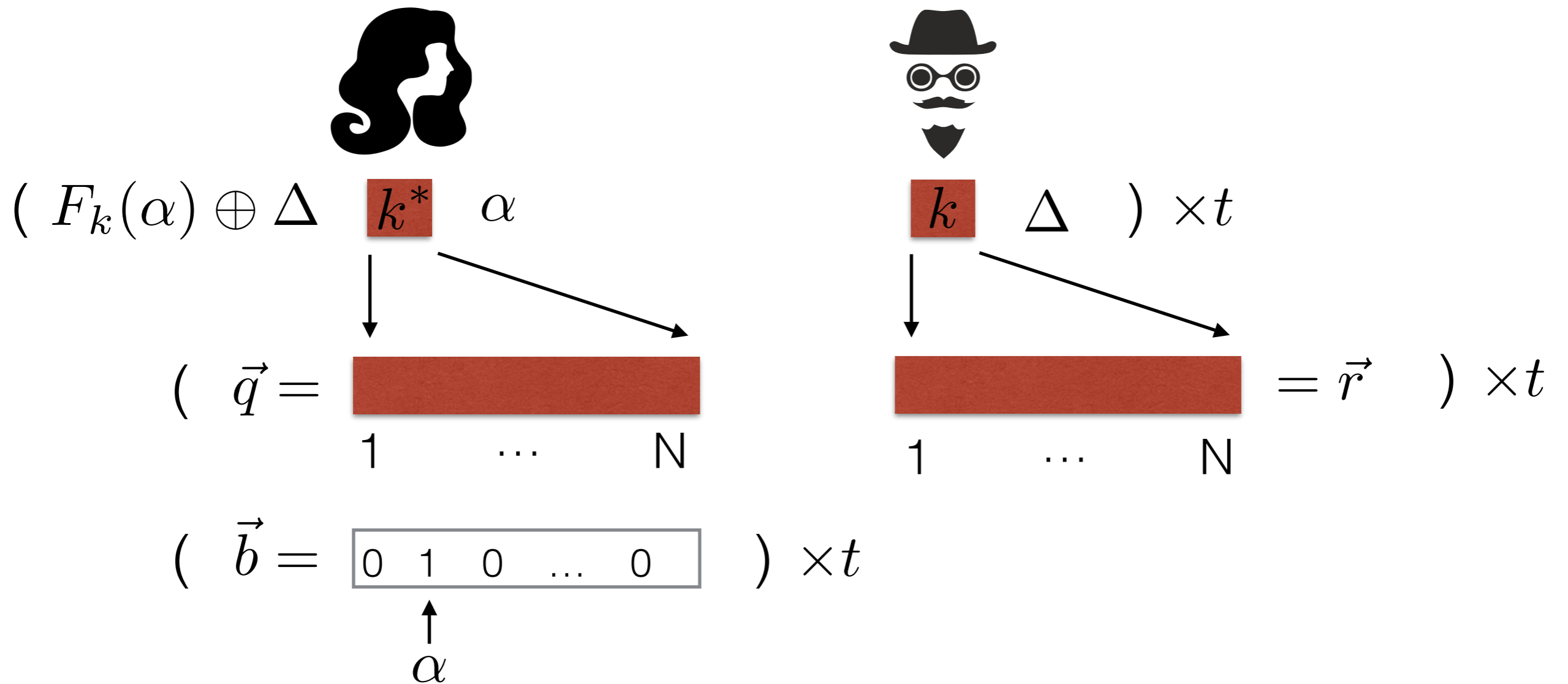


Correlated OT + correlation-robust hash functions \Rightarrow OT [IKNP03]

$$H(r_i \oplus b_i \Delta)$$

$$H(r_i), H(r_i \oplus \Delta)$$

Wrapping Up - PCG for Correlated OT

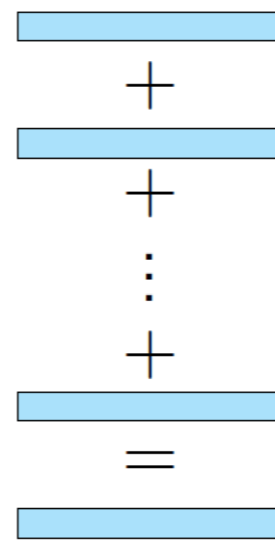
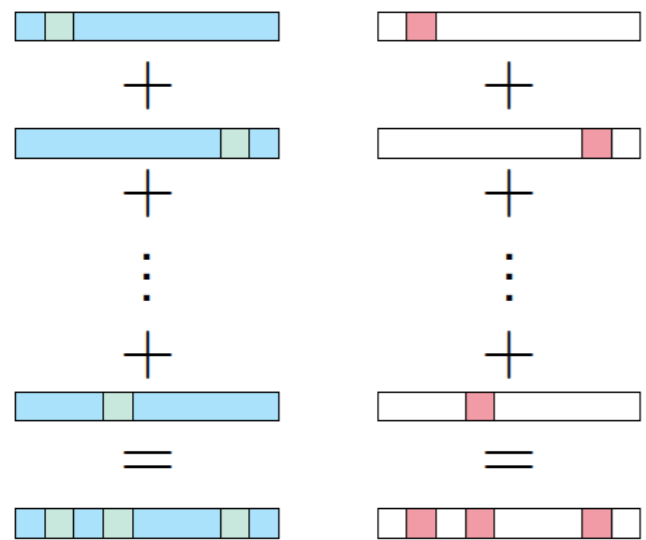


Correlated OT + correlation-robust hash functions => OT [IKNP03]

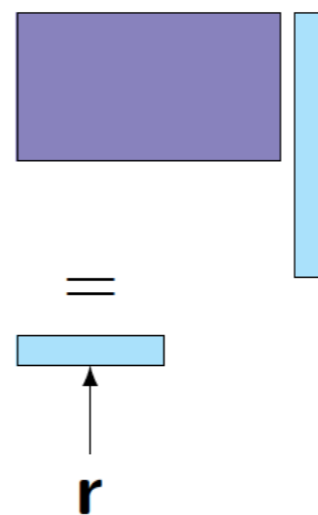
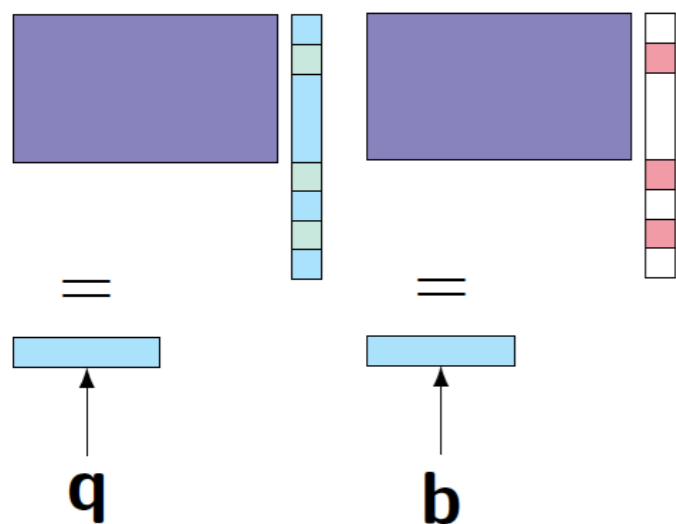
technicality: must use extension fields

$$H(r_i \oplus b_i \Delta) \longleftarrow \longrightarrow H(r_i), H(r_i \oplus \Delta)$$

Optimizing under Stronger Assumptions

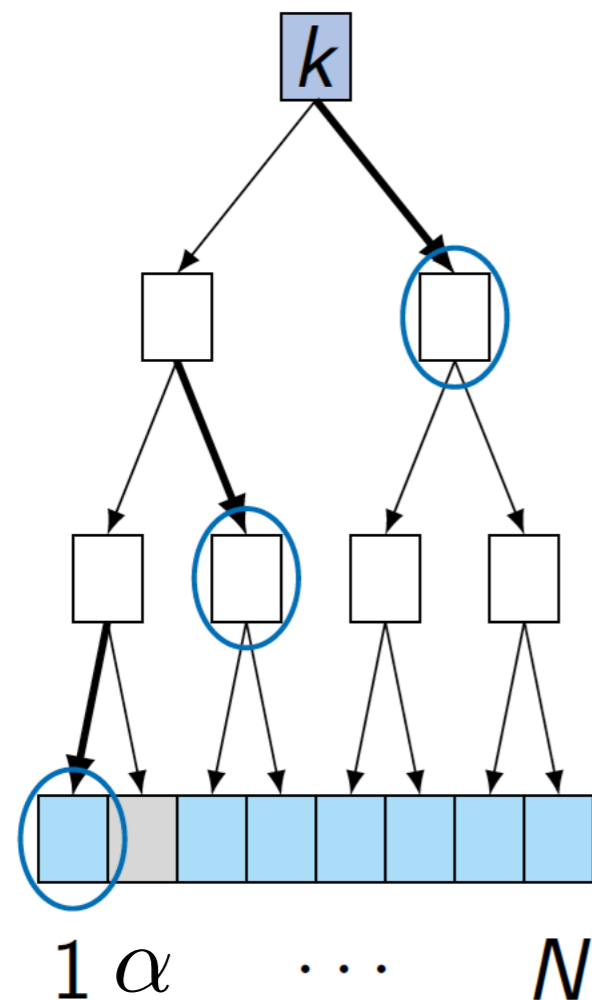


Idea 1:
Regular Syndrome
Decoding



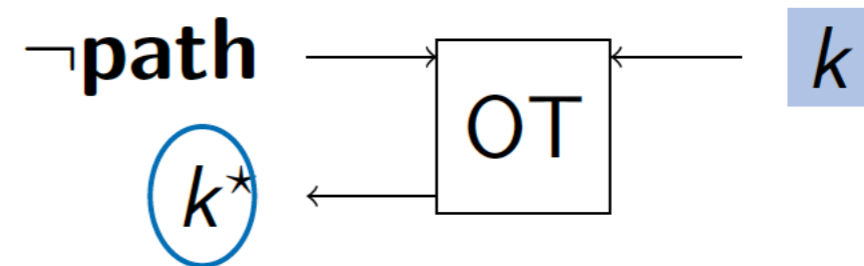
Idea 2:
Quasi-Cyclic
Syndrome Decoding

Distributing the Seed Generation



Strategy: (based on [Ds17])

- ▶ Sender chooses k
- ▶ Receiver receives k^* via chosen OTs:

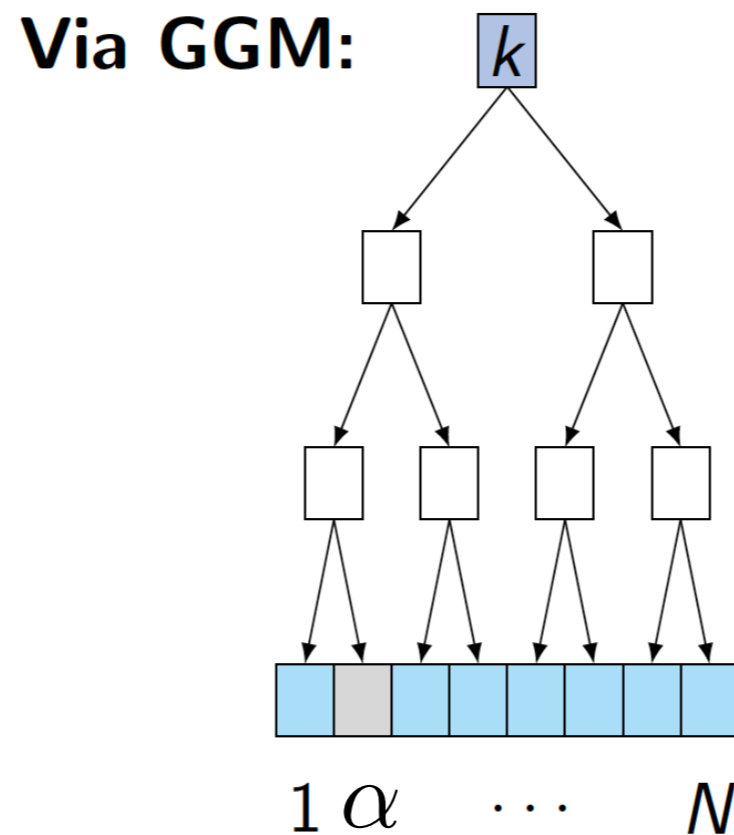


Main observation:

- ▶ Receiver knows α
- ▶ \rightsquigarrow OTs can be executed *in parallel!*

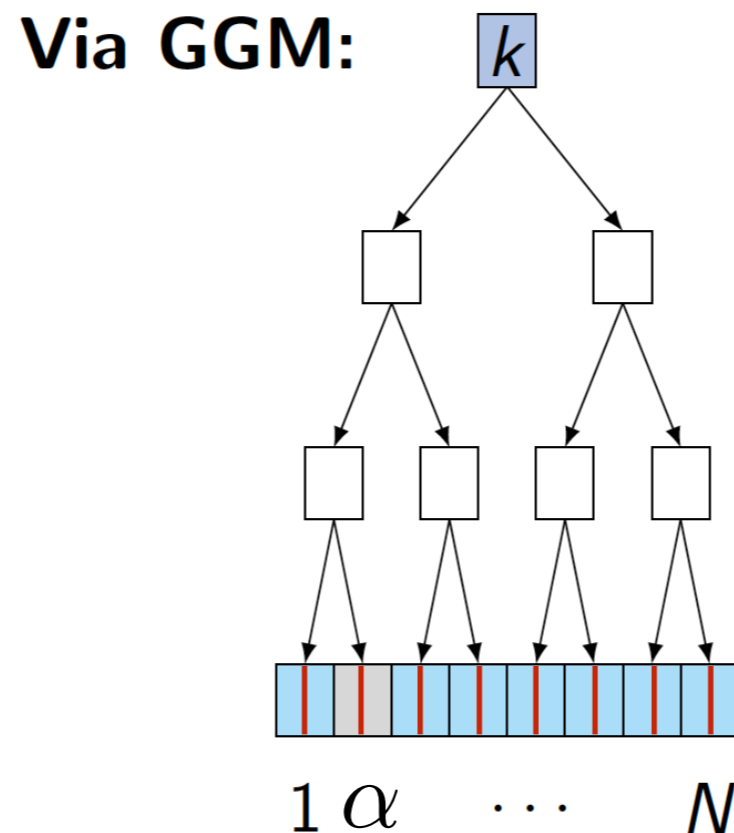
Malicious Security

Core idea: add consistency check inside the PPRF
 \implies extend the domain size from N to $2N$,
use a hash of the odd values to check the punctured key



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Comparison - OT Extension, 128 bits Security

Reference	Rounds	Comm. per random OT	Silent	Active	Based on
[Bea96]	2	poly	✗	✗	OWF
[IKNP03; ALSZ13; KOS15]	3*	128	✗	✓	crh
[KK13] (short strings)	3	≈ 78	✗	✗	crh
[BCGIKS19]	$\log N$	0 – 3	✓	✗	LPN, crh
[BCGIKRS19]	2*	0.1	✓	✓	LPN, crh

*Fiat-Shamir for active security, crh = correlation robust hash function

- ▶ Semi-honest 2-PC w/ 4.2 bits per AND, 30× less than [DKSSZZ17]
- ▶ Improves PSI, malicious MPC
- ▶ Useful for non-interactive secure comp. [IKOPS11; AMPR14; MR17]

Open Problems, Ongoing Works

- Multiparty setting [CRYPTO:BCGIKS20]
- Linear time computation (*ongoing work*)
- Pseudorandom correlation *functions* [FOCS:BCGIKS20]
- Large fields [CRYPTO:BCGIKS20]

...

Thank you for your attention

Questions?

